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## **A NEW COMBINATIVE DISTANCE-BASED ASSESSMENT (CODAS) METHOD FOR MULTI-CRITERIA DECISION-MAKING**

***Abstract.** A key factor to attain success in any discipline, especially in a field which requires handling large amounts of information and knowledge, is decision making. Most real-world decision-making problems involve a great variety of factors and aspects that should be considered. Making decisions in such environments can often be a difficult operation to perform. For this reason, we need multi-criteria decision-making (MCDM) methods and techniques, which can assist us for dealing with such complex problems. The aim of this paper is to present a new **CO**mbinative **D**istance-based **AS**essment (**CODAS**) method to handle MCDM problems. To determine the desirability of an alternative, this method uses the Euclidean distance as the primary and the Taxicab distance as the secondary measure, and these distances are calculated according to the negative-ideal point. The alternative which has greater distances is more desirable in the CODAS method. Some numerical examples are used to illustrate the process of the proposed method. We also perform a comparative sensitivity analysis to examine the results of CODAS and compare it by some existing MCDM methods. These analyses show that the proposed method is efficient, and the results are stable.*

***Keywords:** Multi-criteria decision-making, MCDM, MADM, Euclidean distance, Taxicab distance, CODAS.*

**JEL Classification:** C02, C44, C61, C63, L6

## 1. Introduction

Multi-criteria decision-making (MCDM) is one of the most active fields of interdisciplinary research in management science and operations research (Ho *et al.*, 2010). Multi-attribute decision-making (MADM) and multi-objective decision-making (MODM) are two branches in MCDM. MADM usually involves the discrete decision variables and a limited number of alternatives for evaluation (Jato-Espino *et al.*, 2014). MODM is concerned with identifying the best choice from an infinite set of alternatives under a set of constraints. Each criterion in MODM is associated with an objective, whereas in MADM each criterion is associated with a discrete attribute (Kabir *et al.*, 2014). However, MADM and MCDM have been used to refer the same class of problems in the recent years. In the following, we also use the term MCDM to refer multi-attribute decision-making problems. Fundamentally, intrinsic properties of MCDM make it appealing and practically useful. Some of these properties described by Belton and Stewart (Belton and Stewart, 2002) are as follows: (1) ‘‘MCDM seeks to take explicit account of multiple, conflicting criteria’’, (2) it helps to structure the management problem, (3) it provides a model that can serve as a focus for discussion, and (4) it offers a process that leads to rational, justifiable, and explainable decisions.

Many MCDM methods and techniques have been proposed by researchers in the past decades. Some of the most important ones are weighted sum model (WSM) (Fishburn, 1967), weighted product model (WPM) (Miller and Starr, 1969), weighted aggregated sum product assessment (WASPAS) (Zavadskas *et al.*, 2012), analytical hierarchy process (AHP) (Satty, 1990), ELECTRE (ELimination Et Choix Traduisant la REalité) (Roy, 1968), technique for order of preference by similarity to ideal solution (TOPSIS) (Hwang and Yoon, 1981), preference ranking organization method for enrichment of evaluations (PROMETHEE) (Brans and Vincke, 1985), complex proportional assessment (COPRAS) (Zavadskas and Kaklauskas, 1996), VIKOR (VIseKriterijumska Optimizacija I Kompromisno Resenje) (Opricovic, 1998), MULTIMOORA (multi-objective optimization by ratio analysis plus the full multiplicative form) (Brauers and Zavadskas, 2010), additive ratio assessment (ARAS) (Zavadskas and Turskis, 2010) and evaluation based on distance from average solution (EDAS) (Keshavarz Ghorabae *et al.*, 2015). WSM is probably the most commonly used approach. This method defines the optimal alternative based on the ‘additive utility’ assumption. WPM is very similar to the WSM. This method uses the multiplication of powered weighted ratios (performances) instead of summation of weighted ratios which considered in WSM. WASPAS method was proposed based on the combination of WSM and WPM methods, and has the advantages of both of them. This method has been applied in many real-world MCDM problems (Vafaeipour *et al.*, 2014; Džiugaitė-Tumėnienė and Lapinskaitė, 2014; Petkovic *et al.*, 2015). The AHP, which was proposed by Saaty (Satty, 1981), is based on preferences or weights of importance

of criteria and alternatives with respect to the hierarchical structure of them. We have three levels in the structure of the AHP method. First level is related to the goal of the problem, second level corresponds to the criteria, and third level shows the alternatives. This method involves pair-wise comparisons and therefore is time-consuming when we have numerous criteria and/or alternatives. The original ELECTRE method is labeled as 'ELECTRE I' and the evolutions have continued with ELECTRE II, ELECTRE III, ELECTRE IV, ELECTRE IS and ELECTRE TRI. ELECTRE methods comprise two main procedures: construction of one or several outranking relation(s) and an exploitation procedure. Unlike many other MCDM methods, in the ELECTRE method, it is not assumed that the criteria are mutually independent. One of the disadvantages of the ELECTRE method is about the parameters of discordance and concordance thresholds. It is difficult for a decision maker to provide any justification for the values chosen for these parameters. The TOPSIS method, which was developed by Hwang and Yoon (Satty, 1990), is a value-based compensatory method. This method attempts to rank alternatives according to their distances from the ideal and nadir (positive-ideal and negative-ideal) solutions. However, it does not consider the relative importance of these distances (Opricovic and Tzeng, 2004). PROMETHEE is an MCDM method for ranking a finite set of alternative with respect to some conflicting criteria. PROMETHEE is applicable even when we have simple and efficient information. This method is based on the comparison of alternatives considering the deviations of them on each criterion, and uses preference functions for criteria to determine these deviations. Then the positive and negative preference flows are utilized for appraising and ranking the alternatives (Brans *et al.*, 1986). The COPRAS method is an efficient MCDM method which determines the best alternative according to a ratio based on two measures: benefit criteria performance summation and cost criteria performance summation. The applicability of this method is demonstrated in many real-word MCDM problems (Keshavarz Ghorabae *et al.*, 2014; Hashemkhani Zolfani and Bahrami, 2014; Ecer, 2014; Stefano *et al.*, 2015). The VIKOR method was originally developed by Opricovic (Opricovic, 1998) to solve decision problems with conflicting and non-commensurable criteria (criteria with different units). The alternatives are evaluated according to all established criteria, and solution that is closest to the ideal is the best in this method. The logic of this method is similar to the TOPSIS method. However, there are some significant differences that assessed by Opricovic and Tzeng (2004). The MULTIMOORA method, which was developed by Brauers and Zavadskas (2010), is an extended version of the MOORA (multi-objective optimization by ratio analysis) method (Brauers and Zavadskas, 2006). It consists of three parts, namely the ratio system, the reference point, and the full multiplicative form. This method is efficient and has been applied to many MCDM problems and extended for different environments

like fuzzy and grey environments (Baležentis *et al.*, 2012a; Stanujkic *et al.*, 2012; Baležentis and Baležentis, 2011). The ARAS method is an efficient MCDM method proposed by Zavadskas and Turskis (Zavadskas and Turskis, 2010) for evaluation of microclimate in office rooms. This method has been extended and used in many application fields in the past years (Baležentis *et al.*, 2012b; Dadelo *et al.*, 2012; Stanujkic, 2015). The EDAS method is relatively a new MCDM method which was proposed by Keshavarz Ghorabae, Zavadskas, Olfat and Turskis (2015). The application of this method was examined in the multi-criteria in the multi-criteria inventory ABC classification. Moreover, it was demonstrated that the EDAS method has a good efficiency for dealing with multi-criteria decision-making problems.

All the above-mentioned MCDM methods have advantages and disadvantages which appraising them is not the aim of this paper. In this paper, we want to propose a new method to handle multi-criteria decision-making problems. This method is named CODAS, and has some features that have not been considered in the other MCDM methods. In the proposed method, the overall performance of an alternative is measured by the Euclidean and Taxicab distances from the negative-ideal point. The CODAS uses the Euclidean distance as the primary measure of assessment. If the Euclidean distances of two alternatives are very close to each other, the Taxicab distance is used to compare them. The degree of closeness of Euclidean distances is set by a threshold parameter. The Euclidean and Taxicab distances are measures for  $l^2$ -norm and  $l^1$ -norm indifference spaces, respectively (Yoon, 1987). Therefore, In the CODAS method, we first assess the alternatives in an  $l^2$ -norm indifference space. If the alternatives are not comparable in this space, we go to an  $l^1$ -norm indifference space. To perform this process, we should compare each pair of alternatives. In this study, we present the CODAS method in detail and illustrate the proposed method by using some numerical examples. Moreover, a comparative sensitivity analysis is done to represent the validity and stability of the proposed method. We use different sets of criteria weights and five MCDM methods (WASPAS, COPRAS, TOPSIS, VIKOR and EDAS) to perform this analysis.

The rest of this paper is organized as follows. In Section 2, a new combinative distance-based assessment (CODAS) method is presented in detail. In Section 3, we use some numerical examples to illustrate the process of the CODAS method. In Section 4, a comparative sensitivity analysis is made to demonstrate the efficiency of the proposed method. Conclusions are discussed in the last section.

## **2. Combinative distance-based assessment (CODAS) method**

In this section, we present a new method to deal with multi-criteria decision-making problems. The proposed method is called CODAS, which stands for

**CO**mbinative **D**istance-based **A**ssessment. In this method, the desirability of alternatives is determined by using two measures. The main and primary measure is related to the Euclidean distance of alternatives from the negative-ideal. Using this type of distance requires an  $l^2$ -norm indifference space for criteria. The secondary measure is the Taxicab distance which is related to the  $l^1$ -norm indifference space. It's clear that the alternative which has greater distances from the negative-ideal solution is more desirable. In this method, if we have two alternatives which are incomparable according to the Euclidean distance, the Taxicab distance is used as secondary measure. Although the  $l^2$ -norm indifference space is preferred in the CODAS, two types of indifference space could be considered in its process. Suppose that we have  $n$  alternatives and  $m$  criteria. The steps of the proposed method are presented as follows:

**Step 1.** Construct the decision-making matrix ( $X$ ), shown as follows:

$$X = [x_{ij}]_{n \times m} = \begin{bmatrix} x_{11} & x_{12} & \cdots & x_{1m} \\ x_{21} & x_{22} & \cdots & x_{2m} \\ \vdots & \vdots & \vdots & \vdots \\ x_{n1} & x_{n2} & \cdots & x_{nm} \end{bmatrix}, \quad (1)$$

where  $x_{ij}$  ( $x_{ij} \geq 0$ ) denotes the performance value of  $i$ th alternative on  $j$ th criterion ( $i \in \{1, 2, \dots, n\}$  and  $j \in \{1, 2, \dots, m\}$ ).

**Step 2.** Calculate the normalized decision matrix. We use linear normalization of performance values as follows:

$$n_{ij} = \begin{cases} \frac{x_{ij}}{\max_i x_{ij}} & \text{if } j \in N_b \\ \frac{\min_i x_{ij}}{x_{ij}} & \text{if } j \in N_c \end{cases} \quad (2)$$

where  $N_b$  and  $N_c$  represent the sets of benefit and cost criteria, respectively.

**Step 3.** Calculate the weighted normalized decision matrix. The weighted normalized performance values are calculated as follows:

$$r_{ij} = w_j n_{ij} \quad (3)$$

where  $w_j$  ( $0 < w_j < 1$ ) denotes the weight of  $j$ th criterion, and  $\sum_{j=1}^m w_j = 1$ .

**Step 4.** Determine the negative-ideal solution (point) as follows:

$$ns = [ns_j]_{1 \times m} \quad (4)$$

$$ns_j = \min_i r_{ij} \quad (5)$$

**Step 5.** Calculate the Euclidean and Taxicab distances of alternatives from the negative-ideal solution, shown as follows:

$$E_i = \sqrt{\sum_{j=1}^m (r_{ij} - ns_j)^2} \quad (6)$$

$$T_i = \sum_{j=1}^m |r_{ij} - ns_j| \quad (7)$$

**Step 6.** Construct the relative assessment matrix, shown as follows:

$$Ra = [h_{ik}]_{n \times n} \quad (8)$$

$$h_{ik} = (E_i - E_k) + (\psi(E_i - E_k) \times (T_i - T_k)), \quad (9)$$

where  $k \in \{1, 2, \dots, n\}$  and  $\psi$  denotes a threshold function to recognize the equality of the Euclidean distances of two alternatives, and is defined as follows:

$$\psi(x) = \begin{cases} 1 & \text{if } |x| \geq \tau \\ 0 & \text{if } |x| < \tau \end{cases} \quad (10)$$

In this function,  $\tau$  is the threshold parameter that can be set by decision-maker. It is suggested to set this parameter at a value between 0.01 and 0.05. If the difference between Euclidean distances of two alternatives is less than  $\tau$ , these two alternatives are also compared by the Taxicab distance. In this study, we use  $\tau = 0.02$  for the calculations.

**Step 7.** Calculate the assessment score of each alternative, shown as follows:

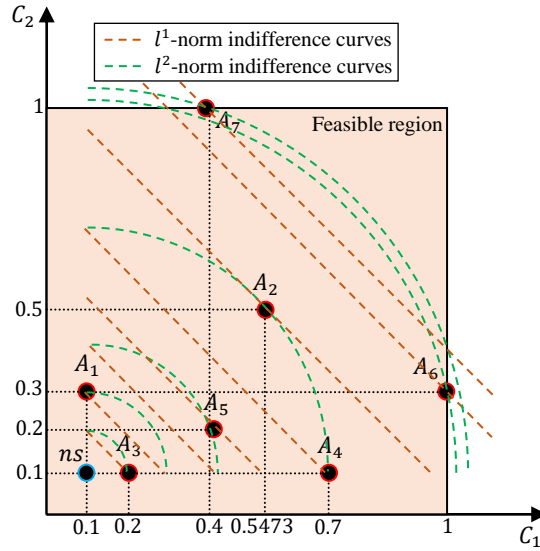
$$H_i = \sum_{k=1}^n h_{ik}, \quad (11)$$

**Step 8.** Rank the alternatives according to the decreasing values of assessment

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score ( $H_i$ ). The alternative with the highest  $H_i$  is the best choice among the alternatives.

To describe the proposed method, we use a simple situation with seven alternatives and two criteria. Suppose that weighted normalized performance values ( $r_{ij}$ ) have been calculated. These values are dimensionless and between 0 and 1. Figure 1 shows the position of all alternatives according to these values.



**Figure 1. A simple graphical example with two criteria**

As can be seen in this figure,  $ns = [0.1 \ 0.1]$  is the negative-ideal point (solution). The Euclidean distances of alternatives from this point are:

$$E_1 = \sqrt{(0.1 - 0.1)^2 + (0.3 - 0.1)^2} = 0.2$$

$$E_2 = \sqrt{(0.5473 - 0.1)^2 + (0.5 - 0.1)^2} = 0.6$$

$$E_3 = \sqrt{(0.2 - 0.1)^2 + (0.1 - 0.1)^2} = 0.1$$

$$E_4 = \sqrt{(0.7 - 0.1)^2 + (0.1 - 0.1)^2} = 0.6$$

$$E_5 = \sqrt{(0.4 - 0.1)^2 + (0.2 - 0.1)^2} = 0.3162$$

$$E_6 = \sqrt{(1 - 0.1)^2 + (0.3 - 0.1)^2} = 0.9220$$

$$E_7 = \sqrt{(0.4 - 0.1)^2 + (1 - 0.1)^2} = 0.9487$$

According to these distances, we can say that the order of alternatives is  $A_3 < A_1 < A_5 < A_2 = A_4 < A_6 < A_7$ . As previously stated, the Euclidean distance is

a measure to compare the alternatives in an  $l^2$ -norm indifference space. In this space we cannot find the difference between  $A_2$  and  $A_4$ . So the Taxicab distance, that is the measure of  $l^1$ -norm indifference space, is used in this case. The Taxicab distances of  $A_2$  and  $A_4$  from the negative-ideal point are:

$$T_2 = |0.5473 - 0.1| + |0.5 - 0.1| = 0.8473$$

$$T_4 = |0.7 - 0.1| + |0.1 - 0.1| = 0.6$$

As can be seen,  $A_2$  has greater Taxicab distance from the negative-ideal point. This fact is clear according to the indifference curves which presented in Figure 1. Therefore, we can say that  $A_2$  is more desirable than  $A_4$ , and the final ranking is  $A_3 < A_1 < A_5 < A_4 < A_2 < A_6 < A_7$ .

### 3. Illustrative examples

To illustrate the process of the CODAS method, we use two examples in this section. The steps of the proposed method are presented through these examples.

#### 3.1. Example 1

This example is adapted from Chakraborty and Zavadskas (2014) which is related to the selection of the most appropriate industrial robot. Five different criteria which are considered in this robot selection problem are: load capacity (in kg), maximum tip speed (in mm/s), repeatability (in mm), memory capacity (in points or steps) and manipulator reach (in mm). Among these criteria, the load capacity, maximum tip speed, memory capacity, and manipulator reach are defined as benefit criteria, and the repeatability is defined as a cost criterion. This problem consists of seven alternatives, and the corresponding data are given in Table 1.

**Table 1. Data of Example 1**

| Alternatives | Weights of criteria<br>Robots     | 0.036         | 0.326             | 0.192         | 0.326           | 0.120             |
|--------------|-----------------------------------|---------------|-------------------|---------------|-----------------|-------------------|
|              |                                   | Load capacity | Maximum tip speed | Repeatability | Memory capacity | Manipulator reach |
| $A_1$        | ASEA-IRB 60/2<br>Cincinnati       | 60            | 0.4               | 2540          | 500             | 990               |
| $A_2$        | Milacrone T3-726                  | 6.35          | 0.15              | 1016          | 3000            | 1041              |
| $A_3$        | Cybotech V15<br>Electric Robot    | 6.8           | 0.10              | 1727.2        | 1500            | 1676              |
| $A_4$        | Hitachi America<br>Process Robot  | 10            | 0.2               | 1000          | 2000            | 965               |
| $A_5$        | Unimation PUMA<br>500/600         | 2.5           | 0.10              | 560           | 500             | 915               |
| $A_6$        | United States<br>Robots Maker 110 | 4.5           | 0.08              | 1016          | 350             | 508               |
| $A_7$        | Yaskawa Electric<br>Motoman L3C   | 3             | 0.1               | 1778          | 1000            | 920               |



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According to Table 1, we can construct the decision matrix. Then the normalized decision matrix is calculated as shown in Table 2.

**Table 2. The normalized decision matrix of Example 1**

| Alternatives | Load capacity | Maximum tip speed | Repeatability | Memory capacity | Manipulator reach |
|--------------|---------------|-------------------|---------------|-----------------|-------------------|
| $A_1$        | 1.000         | 0.200             | 1.000         | 0.167           | 0.591             |
| $A_2$        | 0.106         | 0.533             | 0.400         | 1.000           | 0.621             |
| $A_3$        | 0.113         | 0.800             | 0.680         | 0.500           | 1.000             |
| $A_4$        | 0.167         | 0.400             | 0.394         | 0.667           | 0.576             |
| $A_5$        | 0.042         | 0.800             | 0.220         | 0.167           | 0.546             |
| $A_6$        | 0.075         | 1.000             | 0.400         | 0.117           | 0.303             |
| $A_7$        | 0.050         | 0.800             | 0.700         | 0.333           | 0.549             |

Using weights of criteria that are given in Table 1, the weighted normalized performance values can be calculated, and then the negative-ideal solution is determined. According to the obtained values, the Euclidean and Taxicab distances of alternatives from the negative-ideal solution are also computed. The results are presented in Table 3.

**Table 3. The weighted normalized decision matrix and the negative-ideal solution of Example 1**

| Alternatives            | Load capacity | Maximum tip speed | Repeatability | Memory capacity | Manipulator reach | $E_i$  | $T_i$  |
|-------------------------|---------------|-------------------|---------------|-----------------|-------------------|--------|--------|
| $A_1$                   | 0.0360        | 0.0384            | 0.3260        | 0.0543          | 0.0709            | 0.2593 | 0.3394 |
| $A_2$                   | 0.0038        | 0.1024            | 0.1304        | 0.3260          | 0.0745            | 0.3032 | 0.4510 |
| $A_3$                   | 0.0041        | 0.1536            | 0.2217        | 0.1630          | 0.1200            | 0.2415 | 0.4762 |
| $A_4$                   | 0.0060        | 0.0768            | 0.1283        | 0.2173          | 0.0691            | 0.1947 | 0.3114 |
| $A_5$                   | 0.0015        | 0.1536            | 0.0719        | 0.0543          | 0.0655            | 0.1199 | 0.1606 |
| $A_6$                   | 0.0027        | 0.1920            | 0.1304        | 0.0380          | 0.0364            | 0.1644 | 0.2133 |
| $A_7$                   | 0.0018        | 0.1536            | 0.2282        | 0.1087          | 0.0659            | 0.2087 | 0.3720 |
| Negative-ideal solution | 0.0015        | 0.0384            | 0.0719        | 0.0380          | 0.0364            |        |        |

The relative assessment matrix ( $Ra$ ) and the assessment scores ( $H_i$ ) of alternatives can be calculated by using Table 3 and Eqs. (8) to (10). Table 4 represents the results. It should be noted that, the calculations are performed with  $\tau = 0.02$ .

**Table 4. The relative assessment matrix and the assessment scores of alternatives of Example 1**

|       | $A_1$   | $A_2$   | $A_3$   | $A_4$   | $A_5$  | $A_6$   | $A_7$   | $H_i$   |
|-------|---------|---------|---------|---------|--------|---------|---------|---------|
| $A_1$ | 0.0000  | -0.1554 | 0.0178  | 0.0926  | 0.3181 | 0.2210  | 0.0180  | 0.5122  |
| $A_2$ | 0.1554  | 0.0000  | 0.0364  | 0.2480  | 0.4735 | 0.3764  | 0.1734  | 1.4633  |
| $A_3$ | -0.0178 | -0.0364 | 0.0000  | 0.2116  | 0.4371 | 0.3400  | 0.1370  | 1.0715  |
| $A_4$ | -0.0926 | -0.2480 | -0.2116 | 0.0000  | 0.2255 | 0.1284  | -0.0140 | -0.2125 |
| $A_5$ | -0.3181 | -0.4735 | -0.4371 | -0.2255 | 0.0000 | -0.0971 | -0.3001 | -1.8515 |
| $A_6$ | -0.2210 | -0.3764 | -0.3400 | -0.1284 | 0.0971 | 0.0000  | -0.2030 | -1.1717 |
| $A_7$ | -0.0180 | -0.1734 | -0.1370 | 0.0140  | 0.3001 | 0.2030  | 0.0000  | 0.1887  |

According to the values of assessment scores, the ranking of alternatives is  $A_5 < A_6 < A_4 < A_7 < A_1 < A_3 < A_2$ . Therefore,  $A_2$  (Cincinnati Milacron T3-726) is the best robot with respect to the assessment of the CODAS method.

### 3.2. Example

This example is adapted from Zavadskas and Turskis (2010) and considers the evaluation of microclimate in an office. Six criteria determined for this evaluation process are: the amount of air per head (in  $m^3/h$ ), relative air humidity (in percent), air temperature (in  $^{\circ}C$ ), illumination during work hours (in lx), rate of air flow (in  $m/s$ ), and dew point (in  $^{\circ}C$ ). All of these criteria are defined as benefit criteria except the rate of air flow and the dew point. Fourteen alternatives should be evaluated according to these criteria. The data of this problem are shown in Table 5.

**Table 5. Data of Example 2**

| Weights of Criteria | 0.21                       | 0.16                  | 0.26            | 0.17                           | 0.12             | 0.08      |
|---------------------|----------------------------|-----------------------|-----------------|--------------------------------|------------------|-----------|
| Alternatives        | The amount of air per head | Relative air humidity | Air temperature | Illumination during work hours | Rate of air flow | Dew point |
| $A_1$               | 7.6                        | 46                    | 18              | 390                            | 0.1              | 11        |
| $A_2$               | 5.5                        | 32                    | 21              | 360                            | 0.05             | 11        |
| $A_3$               | 5.3                        | 32                    | 21              | 290                            | 0.05             | 11        |
| $A_4$               | 5.7                        | 37                    | 19              | 270                            | 0.05             | 9         |
| $A_5$               | 4.2                        | 38                    | 19              | 240                            | 0.1              | 8         |
| $A_6$               | 4.4                        | 38                    | 19              | 260                            | 0.1              | 8         |
| $A_7$               | 3.9                        | 42                    | 16              | 270                            | 0.1              | 5         |
| $A_8$               | 7.9                        | 44                    | 20              | 400                            | 0.05             | 6         |
| $A_9$               | 8.1                        | 44                    | 20              | 380                            | 0.05             | 6         |
| $A_{10}$            | 4.5                        | 46                    | 18              | 320                            | 0.1              | 7         |
| $A_{11}$            | 5.7                        | 48                    | 20              | 320                            | 0.05             | 11        |
| $A_{12}$            | 5.2                        | 48                    | 20              | 310                            | 0.05             | 11        |
| $A_{13}$            | 7.1                        | 49                    | 19              | 280                            | 0.1              | 12        |
| $A_{14}$            | 6.9                        | 50                    | 16              | 250                            | 0.05             | 10        |

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According to steps 1 and 2 of the CODAS method and Table 5, we can construct the decision matrix and calculate the normalized performance values using Eq. (2). The normalized decision matrix is shown in Table 6. As can be seen in this table, the maximum values in benefit criteria and the minimum values of cost criteria are transformed to 1. Thus, there is no difference between the dimension (unit of measurement) and the type criteria after normalization.

**Table 6. The normalized decision matrix of Example 2**

| Alternatives | The amount of air per head | Relative air humidity | Air temperature | Illumination during work hours | Rate of air flow | Dew point |
|--------------|----------------------------|-----------------------|-----------------|--------------------------------|------------------|-----------|
| $A_1$        | 0.938                      | 0.920                 | 0.857           | 0.975                          | 0.500            | 0.455     |
| $A_2$        | 0.679                      | 0.640                 | 1.000           | 0.900                          | 1.000            | 0.455     |
| $A_3$        | 0.654                      | 0.640                 | 1.000           | 0.725                          | 1.000            | 0.455     |
| $A_4$        | 0.704                      | 0.740                 | 0.905           | 0.675                          | 1.000            | 0.556     |
| $A_5$        | 0.519                      | 0.760                 | 0.905           | 0.600                          | 0.500            | 0.625     |
| $A_6$        | 0.543                      | 0.760                 | 0.905           | 0.650                          | 0.500            | 0.625     |
| $A_7$        | 0.481                      | 0.840                 | 0.762           | 0.675                          | 0.500            | 1.000     |
| $A_8$        | 0.975                      | 0.880                 | 0.952           | 1.000                          | 1.000            | 0.833     |
| $A_9$        | 1.000                      | 0.880                 | 0.952           | 0.950                          | 1.000            | 0.833     |
| $A_{10}$     | 0.556                      | 0.920                 | 0.857           | 0.800                          | 0.500            | 0.714     |
| $A_{11}$     | 0.704                      | 0.960                 | 0.952           | 0.800                          | 1.000            | 0.455     |
| $A_{12}$     | 0.642                      | 0.960                 | 0.952           | 0.775                          | 1.000            | 0.455     |
| $A_{13}$     | 0.877                      | 0.980                 | 0.905           | 0.700                          | 0.500            | 0.417     |
| $A_{14}$     | 0.852                      | 1.000                 | 0.762           | 0.625                          | 1.000            | 0.500     |

To calculate the negative-ideal solution, we should obtain the weighted normalized performance values first. Table 7 shows the weighted normalized decision-matrix and corresponding negative-ideal solutions. Also, in the last two columns of this table, the Euclidean and Taxicab distances of alternatives from the negative-ideal solution are represented.

**Table 7. The weighted normalized decision matrix and the negative-ideal solution of Example 2**

| Alternatives            | The amount of air per head | Relative air humidity | Air temperature | Illumination during work hours | Rate of air flow | Dew point | $E_i$  | $T_i$  |
|-------------------------|----------------------------|-----------------------|-----------------|--------------------------------|------------------|-----------|--------|--------|
| $A_1$                   | 0.1970                     | 0.1472                | 0.2229          | 0.1658                         | 0.0600           | 0.0364    | 0.1261 | 0.2323 |
| $A_2$                   | 0.1426                     | 0.1024                | 0.2600          | 0.1530                         | 0.1200           | 0.0364    | 0.1085 | 0.2174 |
| $A_3$                   | 0.1374                     | 0.1024                | 0.2600          | 0.1233                         | 0.1200           | 0.0364    | 0.0960 | 0.1825 |
| $A_4$                   | 0.1478                     | 0.1184                | 0.2352          | 0.1148                         | 0.1200           | 0.0444    | 0.0877 | 0.1837 |
| $A_5$                   | 0.1089                     | 0.1216                | 0.2352          | 0.1020                         | 0.0600           | 0.0500    | 0.0457 | 0.0808 |
| $A_6$                   | 0.1141                     | 0.1216                | 0.2352          | 0.1105                         | 0.0600           | 0.0500    | 0.0476 | 0.0945 |
| $A_7$                   | 0.1011                     | 0.1344                | 0.1981          | 0.1148                         | 0.0600           | 0.0800    | 0.0580 | 0.0914 |
| $A_8$                   | 0.2048                     | 0.1408                | 0.2476          | 0.1700                         | 0.1200           | 0.0667    | 0.1550 | 0.3530 |
| $A_9$                   | 0.2100                     | 0.1408                | 0.2476          | 0.1615                         | 0.1200           | 0.0667    | 0.1550 | 0.3496 |
| $A_{10}$                | 0.1167                     | 0.1472                | 0.2229          | 0.1360                         | 0.0600           | 0.0571    | 0.0677 | 0.1429 |
| $A_{11}$                | 0.1478                     | 0.1536                | 0.2476          | 0.1360                         | 0.1200           | 0.0364    | 0.1096 | 0.2444 |
| $A_{12}$                | 0.1348                     | 0.1536                | 0.2476          | 0.1318                         | 0.1200           | 0.0364    | 0.1035 | 0.2272 |
| $A_{13}$                | 0.1841                     | 0.1568                | 0.2352          | 0.1190                         | 0.0600           | 0.0333    | 0.1073 | 0.1915 |
| $A_{14}$                | 0.1789                     | 0.1600                | 0.1981          | 0.1063                         | 0.1200           | 0.0400    | 0.1141 | 0.2063 |
| Negative-ideal solution | 0.1011                     | 0.1024                | 0.1981          | 0.1020                         | 0.0600           | 0.0333    |        |        |

According to the distances given in Table 7, we can calculate the relative assessment matrix and assessment scores related to the steps 6 and 7 of the CODAS method (with  $\tau = 0.02$ ). The results are presented in Table 8.

The calculated assessment values shows that the alternatives is prioritized as  $A_5 < A_6 < A_7 < A_{10} < A_4 < A_3 < A_{13} < A_{12} < A_2 < A_{14} < A_{11} < A_1 < A_9 < A_8$ . Therefore, we can select  $A_8$  as the best alternative with respect to the assessment performed by the CODAS method.

**Table 8. The relative assessment matrix and the assessment scores of alternatives of Example 2**

|          | $A_1$  | $A_2$  | $A_3$  | $A_4$  | $A_5$ | $A_6$  | $A_7$  | $A_8$  | $A_9$  | $A_{10}$ | $A_{11}$ | $A_{12}$ | $A_{13}$ | $A_{14}$ | $H_i$  |
|----------|--------|--------|--------|--------|-------|--------|--------|--------|--------|----------|----------|----------|----------|----------|--------|
| $A_1$    | 0.000  | 0.018  | 0.080  | 0.087  | 0.232 | 0.216  | 0.209  | -0.150 | -0.146 | 0.148    | 0.016    | 0.028    | 0.019    | 0.012    | 0.768  |
| $A_2$    | -0.018 | 0.000  | 0.012  | 0.054  | 0.199 | 0.184  | 0.176  | -0.182 | -0.179 | 0.115    | -0.001   | 0.005    | 0.001    | -0.006   | 0.363  |
| $A_3$    | -0.080 | -0.012 | 0.000  | 0.008  | 0.152 | 0.136  | 0.129  | -0.229 | -0.226 | 0.068    | -0.014   | -0.007   | -0.011   | -0.018   | -0.105 |
| $A_4$    | -0.087 | -0.054 | -0.008 | 0.000  | 0.145 | 0.129  | 0.122  | -0.237 | -0.233 | 0.061    | -0.083   | -0.016   | -0.020   | -0.049   | -0.329 |
| $A_5$    | -0.232 | -0.199 | -0.152 | -0.145 | 0.000 | -0.002 | -0.012 | -0.381 | -0.378 | -0.084   | -0.228   | -0.204   | -0.172   | -0.194   | -2.384 |
| $A_6$    | -0.216 | -0.184 | -0.136 | -0.129 | 0.002 | 0.000  | -0.010 | -0.366 | -0.363 | -0.069   | -0.212   | -0.189   | -0.157   | -0.178   | -2.207 |
| $A_7$    | -0.209 | -0.176 | -0.129 | -0.122 | 0.012 | 0.010  | 0.000  | -0.359 | -0.355 | -0.010   | -0.205   | -0.181   | -0.149   | -0.171   | -2.043 |
| $A_8$    | 0.150  | 0.182  | 0.229  | 0.237  | 0.381 | 0.366  | 0.359  | 0.000  | 0.000  | 0.297    | 0.154    | 0.177    | 0.209    | 0.187    | 2.929  |
| $A_9$    | 0.146  | 0.179  | 0.226  | 0.233  | 0.378 | 0.363  | 0.355  | 0.000  | 0.000  | 0.294    | 0.151    | 0.174    | 0.206    | 0.184    | 2.890  |
| $A_{10}$ | -0.148 | -0.115 | -0.068 | -0.061 | 0.084 | 0.069  | 0.010  | -0.297 | -0.294 | 0.000    | -0.143   | -0.120   | -0.088   | -0.110   | -1.282 |
| $A_{11}$ | -0.016 | 0.001  | 0.014  | 0.083  | 0.228 | 0.212  | 0.205  | -0.154 | -0.151 | 0.143    | 0.000    | 0.006    | 0.002    | -0.005   | 0.568  |
| $A_{12}$ | -0.028 | -0.005 | 0.007  | 0.016  | 0.204 | 0.189  | 0.181  | -0.177 | -0.174 | 0.120    | -0.006   | 0.000    | -0.004   | -0.011   | 0.313  |
| $A_{13}$ | -0.019 | -0.001 | 0.011  | 0.020  | 0.172 | 0.157  | 0.149  | -0.209 | -0.206 | 0.088    | -0.002   | 0.004    | 0.000    | -0.007   | 0.157  |
| $A_{14}$ | -0.012 | 0.006  | 0.018  | 0.049  | 0.194 | 0.178  | 0.171  | -0.187 | -0.184 | 0.110    | 0.005    | 0.011    | 0.007    | 0.000    | 0.364  |

#### 4. Comparative sensitivity analysis

To evaluate the stability and validity of the CODAS method, a comparative sensitivity analysis is performed in this section. The problem that is considered in this analysis is borrowed from Keshavarz Ghorabae *et al.* (2015). In this problem ten alternatives are assessed on seven criteria. To make the analysis, we choose some commonly used MCDM methods for comparing the results of them with the result of the proposed method. The chosen MCDM methods include WASPAS, COPRAS, TOPSIS, VIKOR and EDAS. It should be noted that the TOPSIS method has been proposed in different versions, and we use the version that considered in the research of Opricovic and Tzeng (2004). For this comparative analysis, ten sets of criteria weights are simulated. Data of the MCDM problem and sets of criteria weights are shown in Tables 9 and 10, respectively. In the MCDM problem,  $C_1$  to  $C_3$  are benefit criteria, and  $C_4$  to  $C_7$  are cost criteria. We solve this problem using the CODAS and the selected MCDM methods in the different sets of simulated criteria weights. The results are represented in Table 11.

**Table 9. Data of the MCDM problem for comparative sensitivity analysis**

| Alternatives | Criteria |       |       |       |       |       |       |
|--------------|----------|-------|-------|-------|-------|-------|-------|
|              | $C_1$    | $C_2$ | $C_3$ | $C_4$ | $C_5$ | $C_6$ | $C_7$ |
| $A_1$        | 23       | 264   | 2.37  | 0.05  | 167   | 8900  | 8.71  |
| $A_2$        | 20       | 220   | 2.2   | 0.04  | 171   | 9100  | 8.23  |
| $A_3$        | 17       | 231   | 1.98  | 0.15  | 192   | 10800 | 9.91  |
| $A_4$        | 12       | 210   | 1.73  | 0.2   | 195   | 12300 | 10.21 |
| $A_5$        | 15       | 243   | 2     | 0.14  | 187   | 12600 | 9.34  |
| $A_6$        | 14       | 222   | 1.89  | 0.13  | 180   | 13200 | 9.22  |
| $A_7$        | 21       | 262   | 2.43  | 0.06  | 160   | 10300 | 8.93  |
| $A_8$        | 20       | 256   | 2.6   | 0.07  | 163   | 11400 | 8.44  |
| $A_9$        | 19       | 266   | 2.1   | 0.06  | 157   | 11200 | 9.04  |
| $A_{10}$     | 8        | 218   | 1.94  | 0.11  | 190   | 13400 | 10.11 |

**Table 10. Simulated weights of criteria in different sets**

|        | $C_1$ | $C_2$ | $C_3$ | $C_4$ | $C_5$ | $C_6$ | $C_7$ |
|--------|-------|-------|-------|-------|-------|-------|-------|
| Set 1  | 0.092 | 0.197 | 0.172 | 0.206 | 0.142 | 0.009 | 0.182 |
| Set 2  | 0.215 | 0.156 | 0.174 | 0.172 | 0.092 | 0.151 | 0.041 |
| Set 3  | 0.262 | 0.015 | 0.103 | 0.018 | 0.037 | 0.306 | 0.258 |
| Set 4  | 0.086 | 0.258 | 0.011 | 0.118 | 0.105 | 0.207 | 0.215 |
| Set 5  | 0.054 | 0.139 | 0.127 | 0.184 | 0.201 | 0.215 | 0.079 |
| Set 6  | 0.198 | 0.192 | 0.049 | 0.035 | 0.145 | 0.279 | 0.102 |
| Set 7  | 0.149 | 0.058 | 0.192 | 0.066 | 0.129 | 0.177 | 0.228 |
| Set 8  | 0.303 | 0.174 | 0.044 | 0.047 | 0.082 | 0.268 | 0.082 |
| Set 9  | 0.239 | 0.073 | 0.271 | 0.102 | 0.058 | 0.076 | 0.181 |
| Set 10 | 0.119 | 0.089 | 0.208 | 0.146 | 0.136 | 0.228 | 0.072 |

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**Table 11. The ranking results with different methods in different sets**

| Set No. | Method | $A_1$ | $A_2$ | $A_3$ | $A_4$ | $A_5$ | $A_6$ | $A_7$ | $A_8$ | $A_9$ | $A_{10}$ |
|---------|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| 1       | CODAS  | 2     | 1     | 7     | 10    | 6     | 8     | 3     | 4     | 5     | 9        |
|         | WASPAS | 1     | 2     | 8     | 10    | 6     | 7     | 3     | 4     | 5     | 9        |
|         | COPRAS | 1     | 2     | 8     | 10    | 6     | 7     | 3     | 4     | 5     | 9        |
|         | TOPSIS | 1     | 3     | 9     | 10    | 8     | 7     | 2     | 4     | 5     | 6        |
|         | VIKOR  | 2     | 5     | 8     | 10    | 6     | 7     | 3     | 1     | 4     | 9        |
|         | EDAS   | 1     | 3     | 9     | 10    | 6     | 7     | 2     | 4     | 5     | 8        |
| 2       | CODAS  | 1     | 2     | 6     | 9     | 7     | 8     | 3     | 4     | 5     | 10       |
|         | WASPAS | 1     | 2     | 6     | 10    | 7     | 8     | 3     | 4     | 5     | 9        |
|         | COPRAS | 1     | 2     | 6     | 10    | 7     | 8     | 3     | 4     | 5     | 9        |
|         | TOPSIS | 1     | 3     | 6     | 10    | 8     | 7     | 2     | 4     | 5     | 9        |
|         | VIKOR  | 1     | 5     | 6     | 9     | 7     | 8     | 2     | 3     | 4     | 10       |
|         | EDAS   | 1     | 3     | 6     | 10    | 7     | 8     | 2     | 4     | 5     | 9        |
| 3       | CODAS  | 1     | 2     | 6     | 9     | 7     | 8     | 3     | 4     | 5     | 10       |
|         | WASPAS | 1     | 2     | 6     | 9     | 7     | 8     | 3     | 4     | 5     | 10       |
|         | COPRAS | 1     | 2     | 6     | 9     | 7     | 8     | 3     | 4     | 5     | 10       |
|         | TOPSIS | 1     | 2     | 6     | 9     | 7     | 8     | 3     | 4     | 5     | 10       |
|         | VIKOR  | 1     | 2     | 6     | 9     | 7     | 8     | 3     | 4     | 5     | 10       |
|         | EDAS   | 1     | 2     | 6     | 9     | 7     | 8     | 3     | 4     | 5     | 10       |
| 4       | CODAS  | 1     | 2     | 6     | 10    | 7     | 8     | 3     | 5     | 4     | 9        |
|         | WASPAS | 1     | 2     | 6     | 10    | 7     | 8     | 3     | 5     | 4     | 9        |
|         | COPRAS | 1     | 2     | 6     | 10    | 7     | 8     | 3     | 5     | 4     | 9        |
|         | TOPSIS | 1     | 3     | 7     | 10    | 8     | 9     | 2     | 5     | 4     | 6        |
|         | VIKOR  | 1     | 5     | 7     | 10    | 6     | 8     | 2     | 4     | 3     | 9        |
|         | EDAS   | 1     | 2     | 6     | 10    | 7     | 8     | 3     | 5     | 4     | 9        |
| 5       | CODAS  | 2     | 1     | 6     | 10    | 7     | 8     | 3     | 5     | 4     | 9        |
|         | WASPAS | 1     | 2     | 6     | 10    | 7     | 8     | 3     | 5     | 4     | 9        |
|         | COPRAS | 1     | 2     | 6     | 10    | 7     | 8     | 3     | 5     | 4     | 9        |
|         | TOPSIS | 1     | 2     | 9     | 10    | 8     | 7     | 3     | 5     | 4     | 6        |
|         | VIKOR  | 1     | 5     | 7     | 10    | 6     | 8     | 2     | 4     | 3     | 9        |
|         | EDAS   | 1     | 2     | 6     | 10    | 7     | 8     | 3     | 4     | 5     | 9        |
| 6       | CODAS  | 1     | 2     | 6     | 9     | 7     | 8     | 3     | 4     | 5     | 10       |
|         | WASPAS | 1     | 3     | 6     | 9     | 7     | 8     | 2     | 4     | 5     | 10       |
|         | COPRAS | 1     | 3     | 6     | 9     | 7     | 8     | 2     | 4     | 5     | 10       |
|         | TOPSIS | 1     | 3     | 6     | 9     | 7     | 8     | 2     | 4     | 5     | 10       |
|         | VIKOR  | 1     | 5     | 6     | 8     | 7     | 9     | 2     | 4     | 3     | 10       |
|         | EDAS   | 1     | 3     | 6     | 9     | 7     | 8     | 2     | 4     | 5     | 10       |
| 7       | CODAS  | 1     | 2     | 6     | 9     | 7     | 8     | 4     | 3     | 5     | 10       |
|         | WASPAS | 1     | 2     | 6     | 9     | 7     | 8     | 3     | 4     | 5     | 10       |
|         | COPRAS | 1     | 2     | 6     | 10    | 7     | 8     | 3     | 4     | 5     | 9        |
|         | TOPSIS | 1     | 3     | 6     | 10    | 7     | 8     | 2     | 4     | 5     | 9        |
|         | VIKOR  | 1     | 3     | 8     | 10    | 6     | 7     | 2     | 4     | 5     | 9        |
|         | EDAS   | 1     | 2     | 6     | 10    | 7     | 8     | 3     | 4     | 5     | 9        |
| 8       | CODAS  | 1     | 2     | 6     | 9     | 7     | 8     | 3     | 4     | 5     | 10       |
|         | WASPAS | 1     | 2     | 6     | 9     | 7     | 8     | 3     | 4     | 5     | 10       |
|         | COPRAS | 1     | 2     | 6     | 9     | 7     | 8     | 3     | 4     | 5     | 10       |
|         | TOPSIS | 1     | 3     | 6     | 9     | 7     | 8     | 2     | 4     | 5     | 10       |
|         | VIKOR  | 1     | 3     | 6     | 9     | 7     | 8     | 2     | 5     | 4     | 10       |
|         | EDAS   | 1     | 3     | 6     | 9     | 7     | 8     | 2     | 4     | 5     | 10       |
| 9       | CODAS  | 1     | 2     | 6     | 9     | 7     | 8     | 3     | 4     | 5     | 10       |
|         | WASPAS | 1     | 2     | 6     | 9     | 7     | 8     | 3     | 4     | 5     | 10       |
|         | COPRAS | 1     | 2     | 6     | 10    | 7     | 8     | 3     | 4     | 5     | 9        |
|         | TOPSIS | 1     | 4     | 6     | 10    | 7     | 8     | 2     | 3     | 5     | 9        |
|         | VIKOR  | 2     | 4     | 7     | 10    | 6     | 8     | 3     | 1     | 5     | 9        |
|         | EDAS   | 1     | 4     | 6     | 10    | 7     | 8     | 2     | 3     | 5     | 9        |
| 10      | CODAS  | 2     | 1     | 6     | 10    | 7     | 8     | 3     | 4     | 5     | 9        |
|         | WASPAS | 1     | 2     | 6     | 10    | 7     | 8     | 3     | 4     | 5     | 9        |
|         | COPRAS | 1     | 2     | 6     | 10    | 7     | 8     | 3     | 4     | 5     | 9        |
|         | TOPSIS | 1     | 3     | 7     | 10    | 9     | 8     | 2     | 4     | 5     | 6        |
|         | VIKOR  | 1     | 3     | 6     | 9     | 7     | 8     | 2     | 4     | 5     | 10       |
|         | EDAS   | 1     | 2     | 6     | 10    | 7     | 8     | 3     | 4     | 5     | 9        |

To compare the ranking results obtained from the different methods, the Spearman's rank correlation coefficient ( $r_s$ ) is used. This is a suitable coefficient when we have ordinal variables or ranked variables. Table 12 represents the correlation coefficients that show the association between the results of the proposed method and the selected MCDM methods. If this correlation coefficient is greater than 0.8, the relationship between variables is very strong. As can be seen in Table 12, all values of  $r_s$  are greater than 0.8. Therefore, we can confirm the validity and stability of the results of the CODAS method.

**Table 12. Correlation coefficients between the ranking results of the CODAS and the other methods**

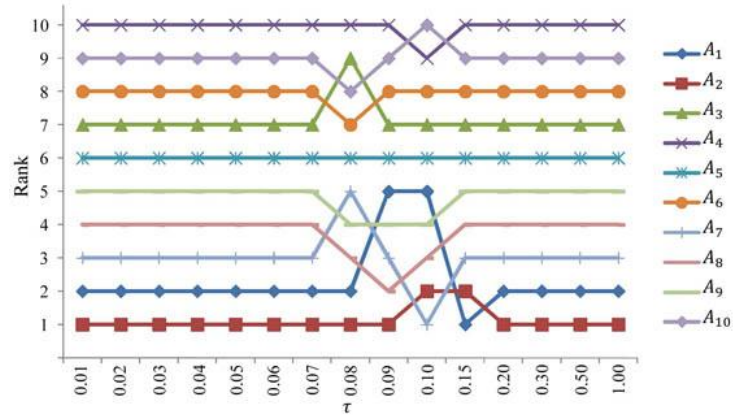
| Method | $r_s$ |       |       |       |       |       |       |       |       |        |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|
|        | Set 1 | Set 2 | Set 3 | Set 4 | Set 5 | Set 6 | Set 7 | Set 8 | Set 9 | Set 10 |
| WASPAS | 0.976 | 0.988 | 1     | 1     | 0.988 | 0.988 | 0.988 | 1     | 1     | 0.988  |
| COPRAS | 0.976 | 0.988 | 1     | 1     | 0.988 | 0.988 | 0.976 | 1     | 0.988 | 0.988  |
| TOPSIS | 0.855 | 0.964 | 1     | 0.915 | 0.867 | 0.988 | 0.952 | 0.988 | 0.952 | 0.879  |
| VIKOR  | 0.830 | 0.927 | 1     | 0.915 | 0.867 | 0.903 | 0.915 | 0.976 | 0.891 | 0.952  |
| EDAS   | 0.927 | 0.976 | 1     | 1     | 0.976 | 0.988 | 0.976 | 0.988 | 0.952 | 0.988  |

As previously mentioned, a threshold parameter ( $\tau$ ) is used in the process of the CODAS method. We suggest a value between 0.01 and 0.05 for this parameter. However, we want to evaluate the effect of changing this parameter on the ranking result of the CODAS methods. According to Table 12, the minimum value of the Spearman's rank correlation coefficient is in the set 1 of criteria weights ( $r_s = 0.83$ ). So this set of criteria weights, which is more sensitive than the other sets, is selected for analysis of changing the threshold parameter. We use fifteen values for this parameter in the range of 0.01 to 1. The ranking results obtained by the CODAS method in different values of  $\tau$  are presented in Table 13. The graphical changes in the ranking of alternatives are also depicted in Figure 2.

**Table 13. Ranking results with different values of  $\tau$**

|          | $\tau$ |      |      |      |      |      |      |      |      |     |       |     |     |     |    |
|----------|--------|------|------|------|------|------|------|------|------|-----|-------|-----|-----|-----|----|
|          | 0.01   | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 | 0.1 | 0.015 | 0.2 | 0.3 | 0.5 | 1  |
| $A_1$    | 2      | 2    | 2    | 2    | 2    | 2    | 2    | 2    | 5    | 5   | 1     | 2   | 2   | 2   | 2  |
| $A_2$    | 1      | 1    | 1    | 1    | 1    | 1    | 1    | 1    | 1    | 2   | 2     | 1   | 1   | 1   | 1  |
| $A_3$    | 7      | 7    | 7    | 7    | 7    | 7    | 7    | 9    | 7    | 7   | 7     | 7   | 7   | 7   | 7  |
| $A_4$    | 10     | 10   | 10   | 10   | 10   | 10   | 10   | 10   | 10   | 9   | 10    | 10  | 10  | 10  | 10 |
| $A_5$    | 6      | 6    | 6    | 6    | 6    | 6    | 6    | 6    | 6    | 6   | 6     | 6   | 6   | 6   | 6  |
| $A_6$    | 8      | 8    | 8    | 8    | 8    | 8    | 8    | 7    | 8    | 8   | 8     | 8   | 8   | 8   | 8  |
| $A_7$    | 3      | 3    | 3    | 3    | 3    | 3    | 3    | 5    | 3    | 1   | 3     | 3   | 3   | 3   | 3  |
| $A_8$    | 4      | 4    | 4    | 4    | 4    | 4    | 4    | 3    | 2    | 3   | 4     | 4   | 4   | 4   | 4  |
| $A_9$    | 5      | 5    | 5    | 5    | 5    | 5    | 5    | 4    | 4    | 4   | 5     | 5   | 5   | 5   | 5  |
| $A_{10}$ | 9      | 9    | 9    | 9    | 9    | 9    | 9    | 8    | 9    | 10  | 9     | 9   | 9   | 9   | 9  |





**Figure 2. Effect of changing the  $\tau$  parameter on ranking of alternatives**

According to Table 13 and Figure 2, we can see the instability in the ranking of alternatives when the  $\tau$  parameter is varied from 0.07 to 0.2. However, changing the  $\tau$  parameter has not a great effect on the ranking of alternatives that can undermine the validity of the results. Therefore, we can confirm the results of the CODAS method.

## 5. Conclusion

Multi-criteria decision-making has increasingly been applied to many real-world problems. Many methods and techniques have also been proposed and improved by researchers in the recent years. In this paper, we have proposed a new combinative distance-based assessment (CODAS) method to handle multi-criteria decision-making problems. To assess the alternatives on multiple criteria, the proposed method uses two types of distances: Euclidean distance and Taxicab distance. These distances are calculated according to the negative-ideal solution. Therefore, the alternative which has greater distances is more desirable. However, in this process, the Euclidean distance is considered as a primary measure and the Taxicab distance is considered as a secondary measure. Two numerical examples have been used to illustrate the CODAS method. Moreover, we have performed a comparative sensitivity analysis to demonstrate the validity and stability of the proposed method. In this analysis, ten sets of criteria weights are simulated and the results of the CODAS method have been compared with the results of some existing MCDM methods. According to the results of this analysis, we can say that the proposed method is efficient to deal with MCDM problems.

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